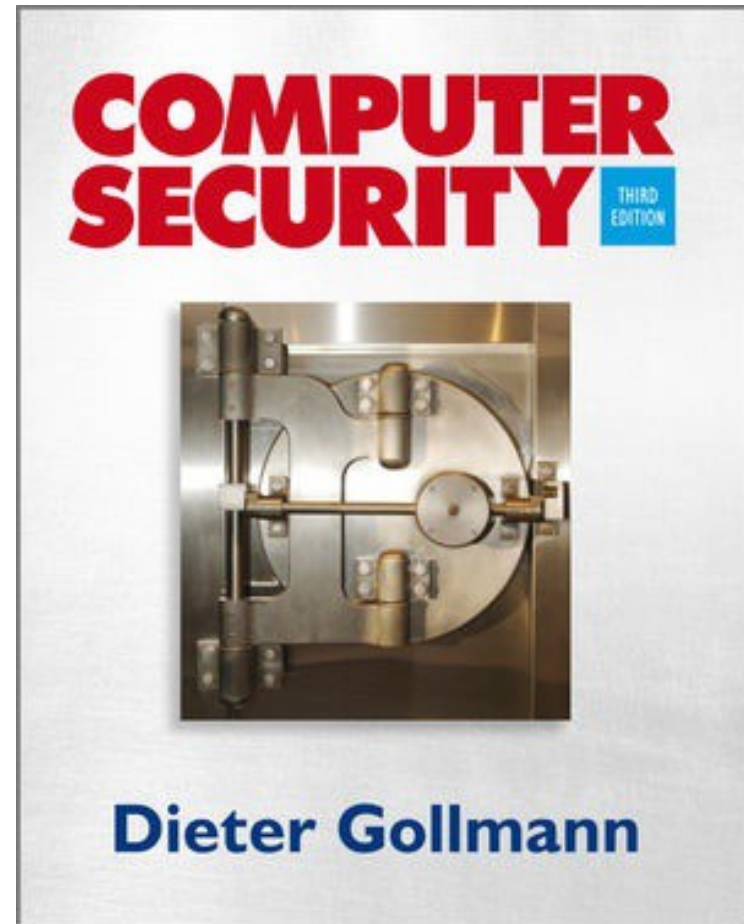


# Computer Security 3e

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Dieter Gollmann



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# Chapter 1: Cryptography

# Cryptography

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- Cryptography is the science and study of secret writing.
- Cryptanalysis is the science and study of methods of breaking ciphers.
- Cryptology: cryptography and cryptanalysis.
- Today [HAC]: Cryptography is the study of mathematical techniques related to aspects of information security, such as confidentiality, data integrity, entity authentication, and data origin authentication.

# Origins of Cryptography

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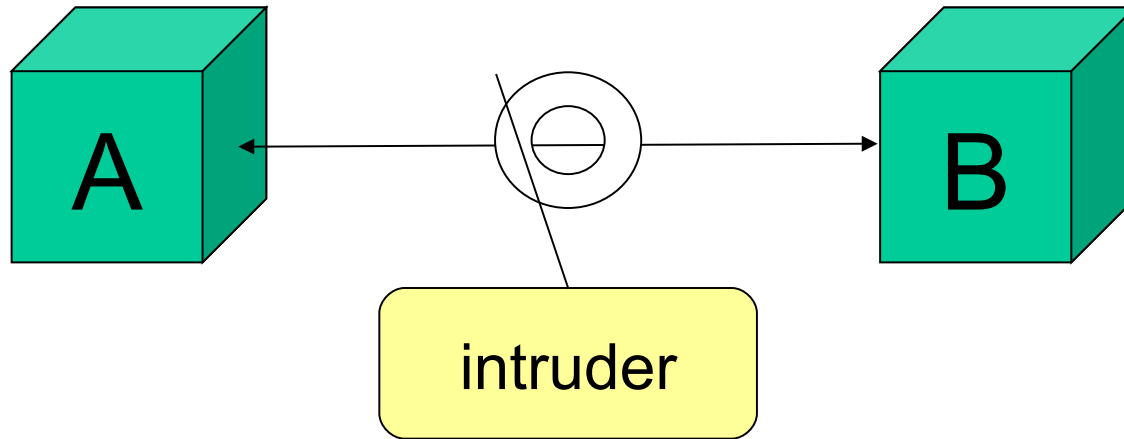
The enemy is an outsider listening to traffic

Two secure end systems communicate over an insecure channel



# Old Paradigm

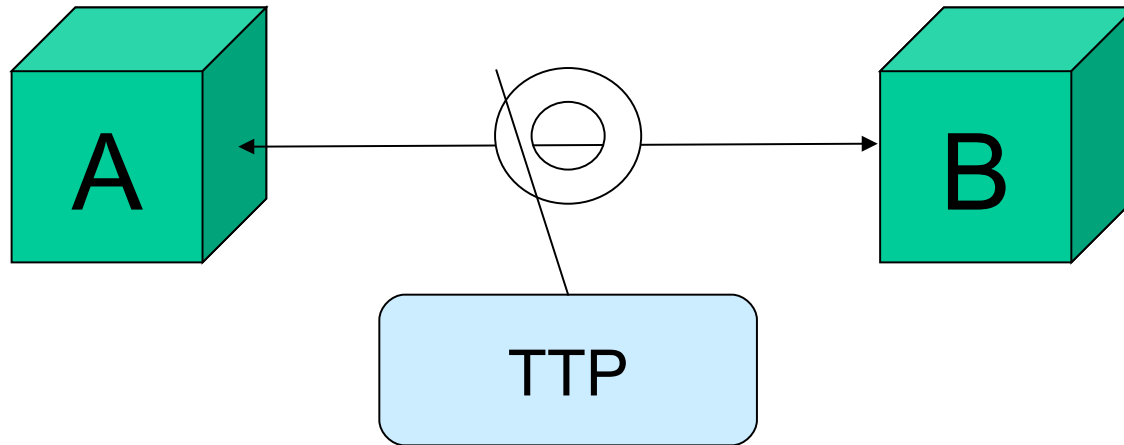
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- *A* and *B* communicate over an insecure channel.
- *A* and *B* trust each other.
- Intruder can read, delete, and insert messages.
- With cryptography, *A* and *B* construct a secure logical channel over an insecure network.

# New Paradigm

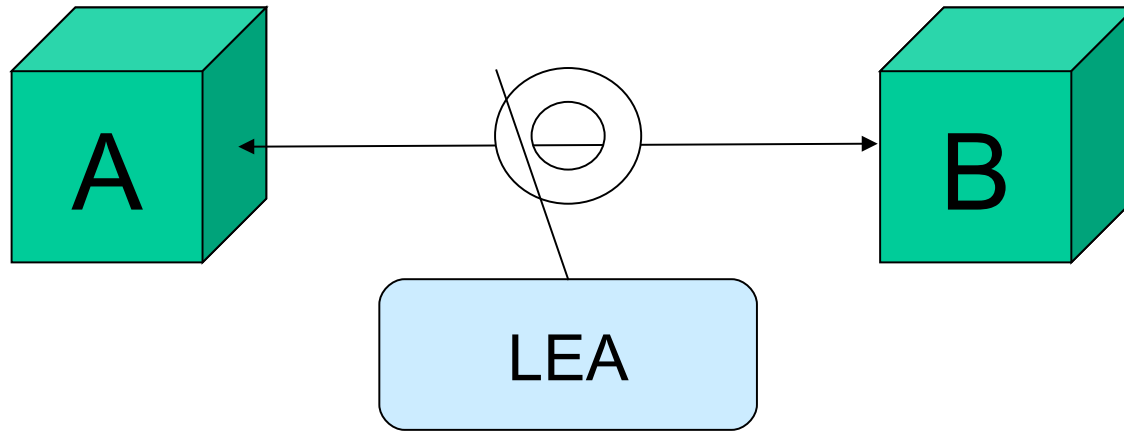
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- **Electronic commerce:** *A* and *B* are customer and merchant; they do not “trust” each other.
- We want protection against insider fraud as much as protection against outsiders.
- **Trusted Third Parties** help settle disputes.

# Law Enforcement

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- In many countries laws regulate how a **law enforcement agency (LEA)** can intercept traffic.
- **Key recovery** makes cryptographic keys available to their owner.
- **Key escrow** makes keys available to a LEA.

# Communications Security

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- Security services provided by cryptographic mechanisms:
- **Data confidentiality**: encryption algorithms hide the content of messages;
- **Data integrity**: integrity check functions provide the means to detect whether a document has been changed;
- **Data origin authentication**: message authentication codes or digital signature algorithms provide the means to verify the source and integrity of a message.



# Data Integrity & Authentication

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- Data origin authentication includes data integrity: a message that has been modified in transit no longer comes from the original source.
- Data integrity includes data origin authentication: when the sender's address is part of the message, you have to verify the source of a message when verifying its integrity.
- Under the assumptions made, data integrity and data origin authentication are equivalent.
- In other applications a separate notion of data integrity makes sense, e.g. for file protection in anti-virus software.

# Cryptographic Keys

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- Cryptographic algorithms use **keys** to protect data.
- **Kerckhoffs' principle**: do not rely on the secrecy of algorithms; the key should be the only secret that needs protection.
  - De facto standardisation and open evaluation of public algorithms is today the norm.
- **Key management issues**:
  - Where are keys generated?
  - How are keys generated?
  - Where are keys stored?
  - How do they get there?
  - Where are the keys actually used?
  - How are keys revoked and replaced?

# Shifting the Goal Post

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- Cryptographic keys are sensitive data stored in a computer system; access control mechanisms in the computer system have to protect these keys.
- Lesson: cryptography is rarely ever the solution to a security problem; cryptography is a translation mechanism, usually converting a communications security problem into a key management problem and ultimately into a computer security problem.

# Shifting the Goal Post

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# Crypto in Computer Security

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- **Vault** for locking away secrets: unlocked with a key when putting data in or taking data out; implemented by **symmetric encryption** mechanisms.
- **Transparent vault** (cf. public lottery draws): everyone sees what is in the vault, a **private key** is need to fill it; a **public key** is the unique serial number of the vault.
- **Private letter box**: anybody can drop documents, only the owner can open it with a **private key**; a **public key** is the serial number of the letter box; like the feature above implemented using **public key cryptography**.
- When a document leaves your control, save a **fingerprint** so that you could detect any eventual later changes; can be implemented with **hash functions**.

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# Integrity Check Functions

# Integrity Protection – Example

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- To protect a program  $x$ , compute its hash  $h(x)$  in a clean environment and store it in a place where it cannot be modified, e.g. on CD-ROM.
- Protection of the hash value is important; computing the hash value requires no secret information, so anybody can create a valid hash for a given file.
- To check whether the program has been modified, re-compute the hash value and compare it with the value stored.

# One-way Functions

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- Requirements on a one-way function  $h$ :
- **Ease of computation**: given  $x$ , it is easy to compute  $h(x)$ .
- **Compression**:  $h$  maps inputs  $x$  of arbitrary bitlength to outputs  $h(x)$  of a fixed bitlength  $n$ .
- **Pre-image resistance (one-way)**: given a value  $y$ , it is computationally infeasible to find an input  $x$  so that  $h(x) = y$ .



# Collisions

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- The application just described needs more than the one-way property of  $h$ .
- We are not concerned about an attacker reconstructing the program from the hash.
- We are concerned about attackers who change program  $x$  to  $x'$  so that  $h(x') = h(x)$ .
- Then, our integrity protection mechanism would fail to detect the change.
- We say there is a **collision** when two inputs  $x$  and  $x'$  map to the same hash.

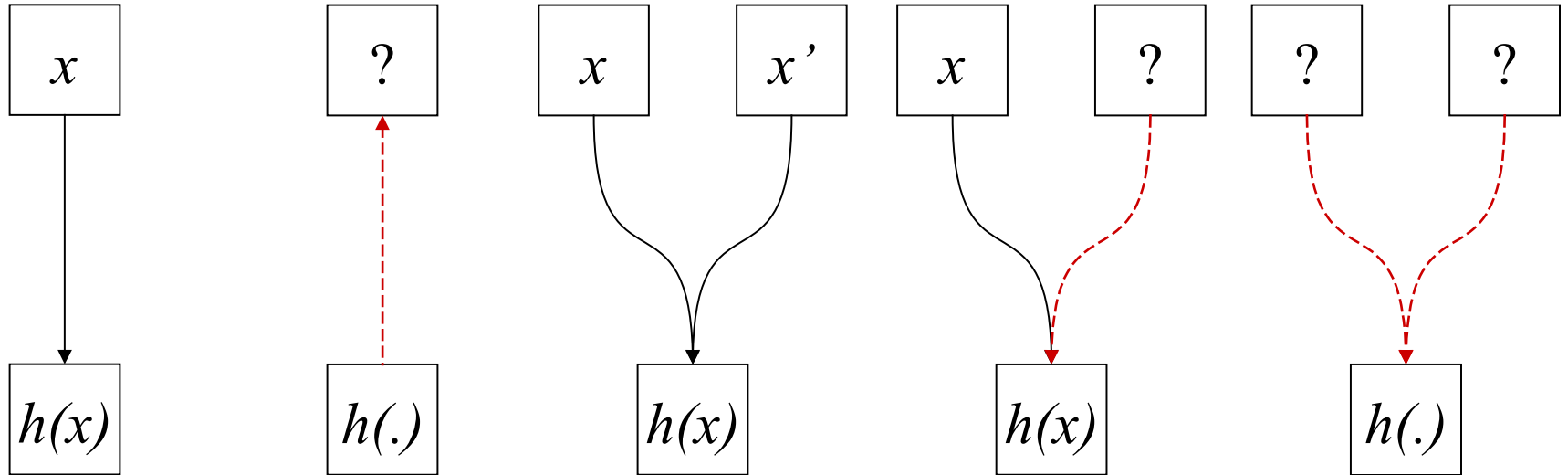
# Collision Resistance

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- Integrity protection requires collision-resistant hash functions; we distinguish between:
- **2nd pre-image resistance (weak collision resistance)**: given an input  $x$  and  $h(x)$ , it is computationally infeasible to find another input  $x'$ ,  $x \neq x'$ , with  $h(x) = h(x')$ .
- **Collision resistance (strong collision resistance)**: it is computationally infeasible to find any two inputs  $x$  and  $x'$ ,  $x \neq x'$ , with  $h(x) = h(x')$ .

# Properties of One-way Functions

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ease of  
computation

pre-image  
resistance

collision

2<sup>nd</sup> pre-image  
resistance

collision  
resistance

# Manipulation Detection Codes

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- Manipulation detection code (MDC, also modification detection code, message integrity code): used to detect changes to a document.
- Two types of MDCs:
- **One-way hash function (OWHF)**: ease-of-computation, compression, pre-image resistance, and 2nd pre-image resistance.
- **Collision resistant hash function (CRHF)**: compression, ease-of-computation, 2nd pre-image resistance, and collision resistance.

# Checksums

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- The result of applying a hash function is called **hash value**, **message digest**, or **checksum**.
- The last term creates frequent confusion .
- In communications, checksums often refer to error correcting codes, typically a **cyclic redundancy check (CRC)**.
- Checksums used by anti-virus products, on the other hand, must not be computed with a CRC but with a cryptographic hash function.

# Construction

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- Pattern for the design of fast hash functions:
- Core of the hash function is a **compression function**  $f$  that works on fixed size input blocks.
- An input  $x$  of arbitrary length is broken up into blocks  $x_1, \dots, x_m$  of the given block size; last block has to be padded.
- Repeatedly apply the compression function: with a (fixed) initial value  $h_0$ , compute  $h_i = f(x_i || h_{i-1})$  for  $i=1, \dots, m$ , take  $h_m$  as the hash value of  $x$ .
- The symbol  $||$  denotes concatenation.

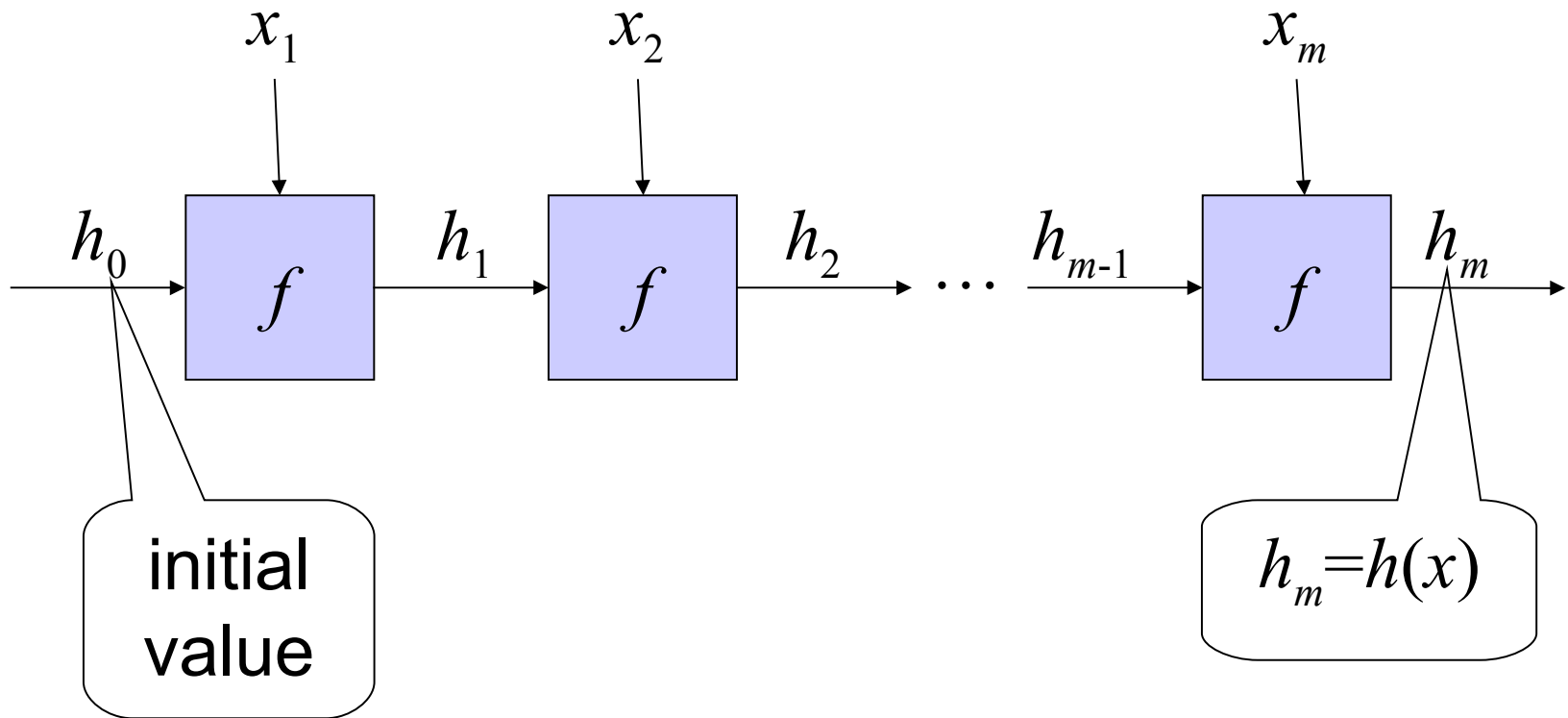
# Frequently Used Hash Functions

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- **MD4**: weak, it is computationally feasible to find meaningful collisions.
- **MD5**: standard choice in Internet protocols, so broken and no longer recommended.
- Secure Hash Algorithm (**SHA-1**): designed to operate with the US Digital Signature Standard (DSA); 160-bit hash value; collision attacks reported.
- **RIPEND-160**: hash function frequently used by European cryptographic service providers.
- **SHA-256**: when longer hash values are advisable.

# Construction

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# Message Authentication Codes

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- In communications, we cannot rely on secure storage to protect hash values.
- Use secrets instead: compute a MAC  $h_k(x)$  from the message  $x$  and a secret key  $k$ .
- To verify a message, receiver has to share the secret key used to compute the MAC with the sender.
- A MAC must have the compression and ease-of-computation property, and an additional **computation resistance** property:
  - For any fixed value of  $k$  unknown to the adversary, given a set of values  $(x_i, h_k(x_i))$ , it is computationally infeasible to compute  $h_k(x)$  for any new input  $x$ .

# HMAC (simplified)

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- A MAC algorithm can be derived from a MDC algorithm  $h$  using the HMAC construction:
- For a given key  $k$  and message  $x$ , compute

$$\text{HMAC}(x) = h(k||p_1||h(k||p_2||x))$$

where  $p_1$  and  $p_2$  are bit strings (padding) that extend  $k$  to a full block length of the compression function used in  $h$ .

- Details of HMAC specified in RFC 2104.

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# Digital signatures

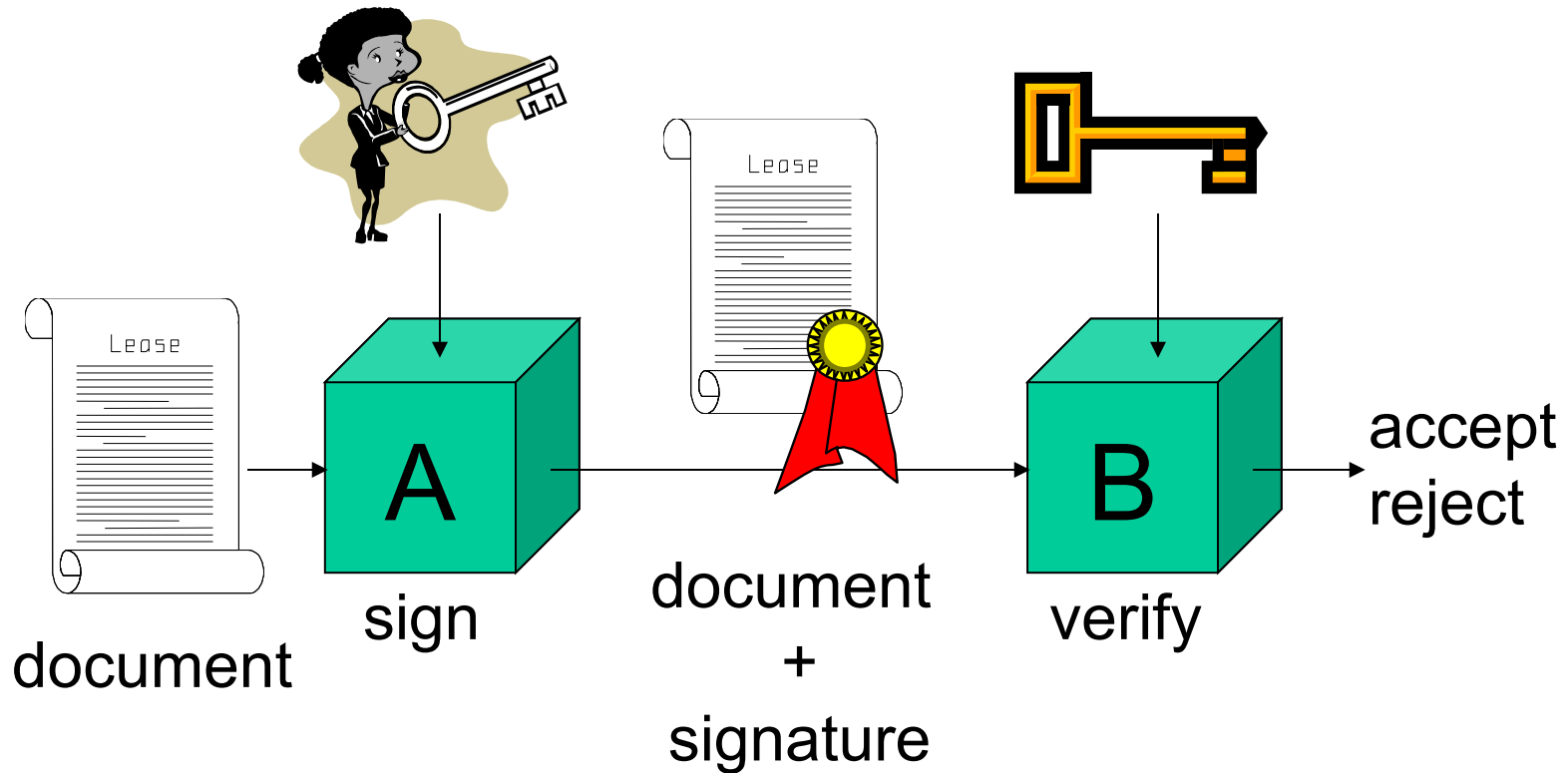
# Digital Signature Mechanisms

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- A MAC cannot be used as evidence that should be verified by a third party.
- Digital signatures used for non-repudiation, data origin authentication and data integrity services, and in some authentication exchange mechanisms.
- Digital signature mechanisms have three components:
  - key generation
  - signing procedure (private)
  - verification procedure (public)

# Digital Signatures

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# Digital Signatures

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- $A$  has a **public verification key** and a **private signature key** ( public key cryptography).
- $A$  uses her private key to compute her signature on document  $m$ .
- $B$  uses a public verification key to check the signature on a document  $m$  he receives.
- At this technical level, digital signatures are a cryptographic mechanism for associating documents with verification keys.
- To get an authentication service that links a document to  $A$ 's name (identity) and not just a verification key, we require a procedure for  $B$  to get an authentic copy of  $A$ 's public key.

# RSA Signatures

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- RSA (Rivest, Shamir, Adleman) algorithm can be used for signing and for encryption.
- This property peculiar to RSA has led to many misconceptions about digital signatures and public key cryptography.
- **Key generation:**
  - User  $A$  picks two prime numbers  $p, q$ .
  - Private signature key: an integer  $d$  with  $\gcd(d, p-1) = 1$  and  $\gcd(d, q-1) = 1$ .
  - Public verification key:  $n = p \cdot q$  and an integer  $e$  with  $e \cdot d = 1 \pmod{\text{lcm}(p-1, q-1)}$ .

# RSA Signatures

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- **Signing:** signer  $A$  hashes the document  $m$  so that  $0 < h(m) < n$  and computes signature  $s = h(m)^d \bmod n$ .
- **Verification:** verifier uses a verification key  $(n, e)$  and checks  $s^e \stackrel{?}{=} h(m) \bmod n$ .
- For a correct signature, this equation holds because
$$s^e = h(m)^{d \cdot e} = h(m) \bmod n.$$
- Hash function adds format check on message.
- Otherwise, **existential forgeries** are possible:
  - Pick signature  $s$ , construct 'message'  $m = s^e \bmod n$ .
  - $m$  is random bit string; can be detected by format check on  $m$ .



# Performance Gains

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- Signature verification is particularly quick for specific ‘small’ public verification keys, e.g.  $e = 2^{16} + 1$ .
  - Performance measurements for RSA often show much smaller values for verification than for signing; in such cases a ‘small’ public key had been used.
- **Signatures with message recovery**: RSA has modes where short documents can be recovered from the signature and do not have to be transmitted separately.
  - Relevant e.g. for smart card applications.

# Factorization & RSA

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- Factorization: given an integer  $n$ , find its prime factors.
- Finding small factors is “easy”.
- Testing for primality is “easy”.
- Factoring an RSA modulus  $n = p.q$  is “difficult”.
- When the public modulus  $n = p.q$  can be factored, the security of RSA is compromised.
- There exists no proof that the security of RSA is equivalent to the difficulty of factoring.

# MACs & Digital Signatures

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- MACs and digital signatures are authentication mechanisms.
- MAC: verifier needs the secret used to compute the MAC; MAC unsuitable as evidence with a third party.
  - Third party would need the secret.
  - Third party cannot distinguish between the parties knowing the secret.
- Digital signatures can be used as evidence with a third party.
- The term “non-repudiation” was coined to distinguish the features of authentication based on digital signatures from MAC-based authentication.

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# Encryption

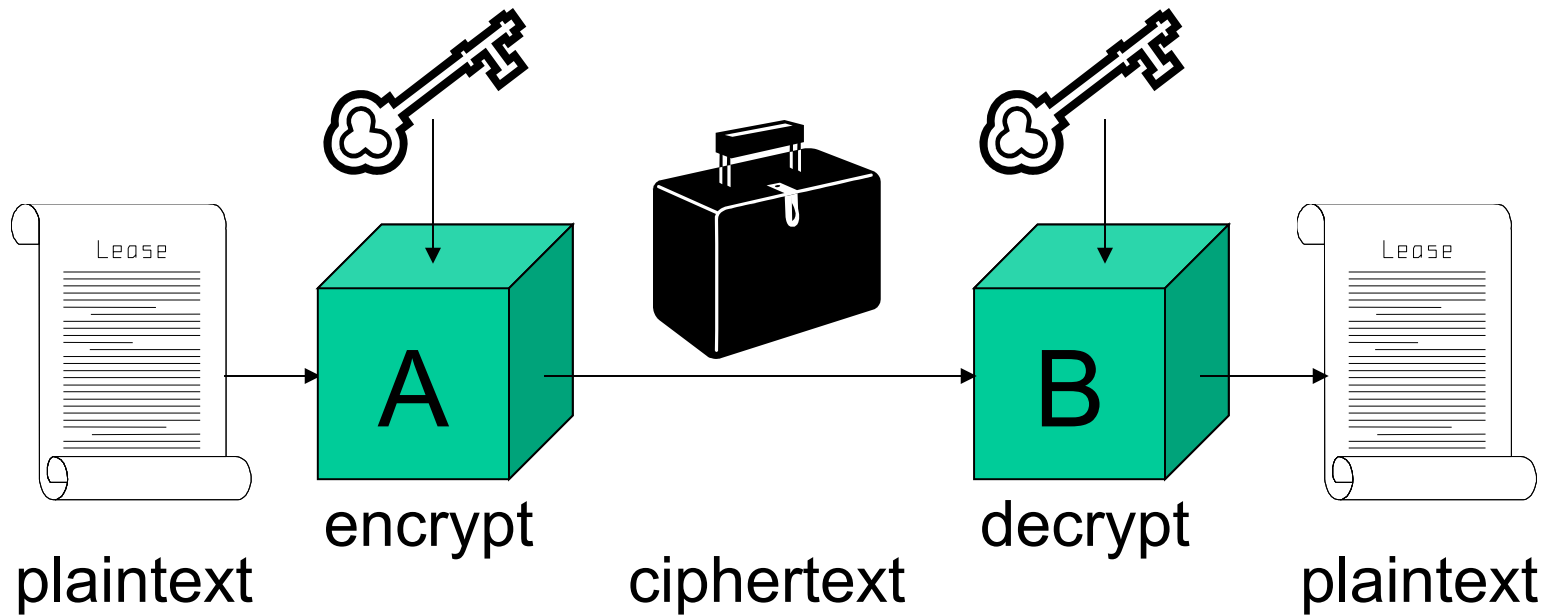
# Terminology

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- **Encryption**: plaintext (clear text)  $x$  is converted into a ciphertext under the control of a key  $K$ .
  - We write  $eK(x)$ .
- **Decryption** with key  $K$  computes the plaintext from the ciphertext  $y$ .
  - We write  $dK(y)$ .
- **Symmetric ciphers**: the decryption key is essentially the same as the encryption key.
- **Asymmetric ciphers**: it is computationally infeasible to derive the **private decryption key** from the corresponding **public encryption key**.

# Symmetric Key Encryption

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# Symmetric Key Cryptography

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- Protects documents on the way from  $A$  to  $B$ .
- $A$  and  $B$  need to share a key.
- $A$  and  $B$  have to keep their keys secret (secret key cryptography).
- There has to be a procedure whereby  $A$  and  $B$  can obtain their shared key.
- For  $n$  parties to communicate directly, about  $n^2$  keys are needed.

# Block Ciphers & Stream Ciphers

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- **Block ciphers**: encrypt sequences of “long” data blocks without changing the key.
  - Security relies on design of encryption function.
  - Typical block length: 64 bits, 128 bits.
- **Stream ciphers**: encrypt sequences of “short” data blocks under a changing key stream.
  - Security relies on design of key stream generator.
  - Encryption can be quite simple, e.g. XOR.
  - Typical block length: 1 bit, 1 byte.



# Algorithms

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- DES (more in a moment)
- AES (more in a moment)
- Triple-DES: ANSI X9.45, ISO 8372
- FEAL
- IDEA
- SAFER
- Blowfish, Mars, Serpent, ...
- and many more

# Advanced Encryption Standard

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- Public competition to replace DES: 56-bit keys and 64-bit data blocks no longer adequate.
- Rijndael (pronounce as “Rhine-doll”) nominated as the new Advanced Encryption Standard (AES) in 2001 [FIPS-197].
- Designed by Vincent Rijmen & Joan Daemen.
- Versions for 128-bit, 192-bit, and 256-bit data and key blocks (all combinations of block length and key length are possible).
- Rijndael is not a Feistel cipher.

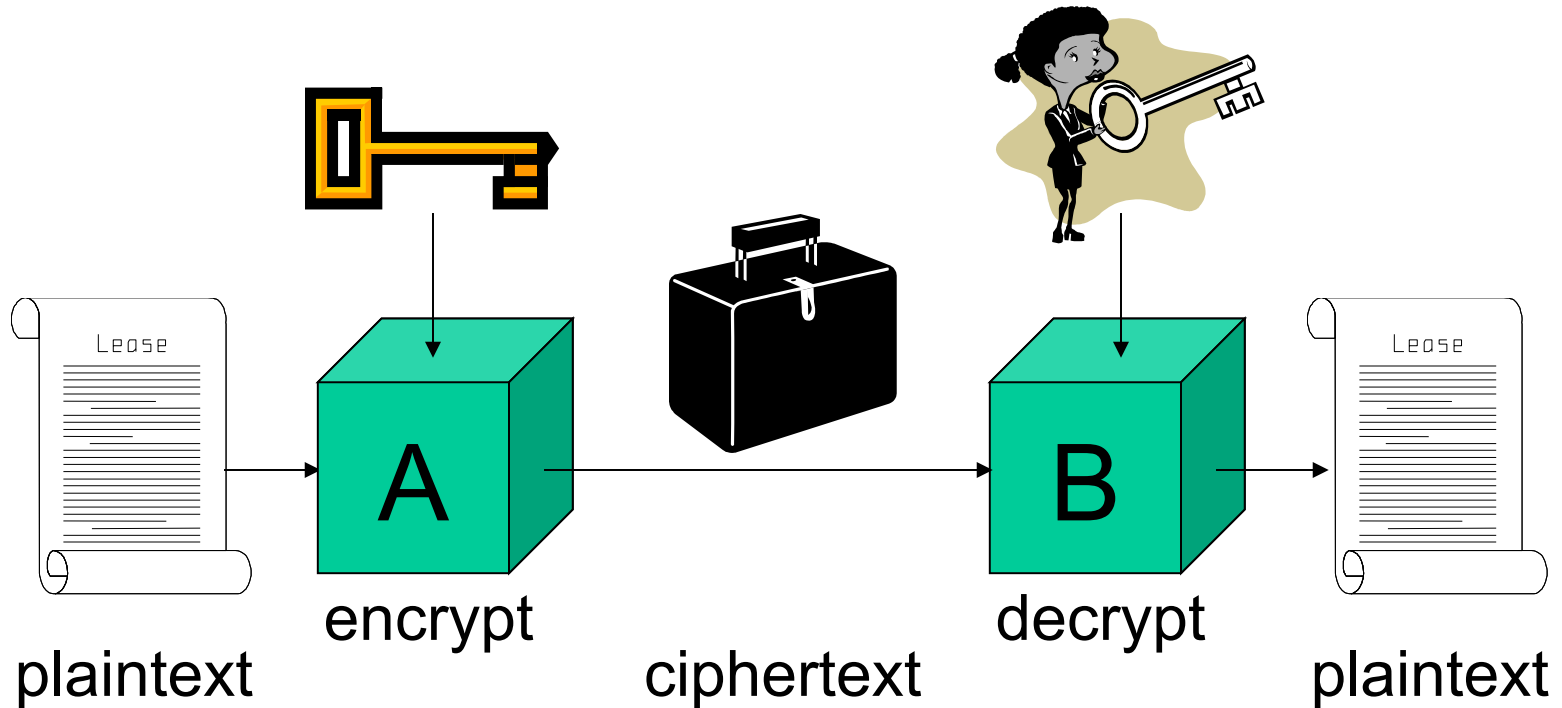
# Public key Encryption

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- Proposed in the open literature by Diffie & Hellman in 1976.
- Each party has a **public encryption key** and a **private decryption key**.
- Computing the private key from the public key should be computationally infeasible.
- The public key need not be kept secret but it is not necessarily known to everyone.
- There exist applications where access to public keys is restricted.

# Encryption with Public Keys

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# Public key Encryption

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- Protects documents on the way from  $A$  to  $B$ .
- $B$  has a **public encryption key** and a **private decryption key**.
- A procedure is required for  $A$  to get an authentic copy of  $B$ 's public key (**need not be easier than getting a shared secret key**).
- For  $n$  parties to communicate,  $n$  key pairs are needed.

# Public Key Infrastructures

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- “With public key cryptography, you can send messages securely to a stranger”.
- This is not really true; how do you know who has got the private key corresponding to the public key you are using?
- How do you get a public key for a party you want to send a message to?
- Additional “public key infrastructures” are needed to link persons to keys.

# RSA Encryption

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- We have already discussed the RSA (Rivest, Shamir, Adleman) signature algorithm.
- RSA encryption is based on the same principles.
- **Key generation:**
  - User  $A$  picks two prime numbers  $p, q$ .
  - Public encryption key:  $n = p \cdot q$  and an integer  $e$  with  $\gcd(e, p-1) = 1$  and  $\gcd(e, q-1) = 1$ .
  - Private decryption key: an integer  $d$  with  $e \cdot d = 1 \pmod{\text{lcm}(p-1, q-1)}$ .

# RSA Encryption

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- Messages are broken into message blocks  $m_i$  so that  $0 < m_i < n$ .
- **Encryption**: sender  $A$  takes a message block  $m$  and computes the ciphertext  $c = m^e \bmod n$ .
- **Decryption**: receiver uses its decryption exponent  $d$  and computes  $m = c^d \bmod n$ .
- Note:  $c^d = m^{e \cdot d} = m \bmod n$ .
- Don't be deceived by the simplicity of RSA, proper implementation can be quite tricky.



# Padding

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- RSA is a block cipher; keys are chosen so that the block length is 1024 bit (or 2048, 4096, ...)
- When encrypting a message, padding may have to be added to make the message length a multiple of the block length.
- Padding can defeat some attacks: when decrypting a message, the receiver can check the padding data and discard plaintexts with syntactically incorrect padding.